

# Factors influencing the stormwater quality model of sewer networks and a case study of Louis Fargue urban catchment in Bordeaux, France

Congcong Sun <sup>1,\*</sup>, Benjamí Parellada <sup>1</sup>, Jing Feng <sup>2</sup>, Vicenç Puig <sup>1</sup> and Gabriela Cembrano <sup>1,3</sup>

<sup>1</sup> Advanced Control Systems Group at the Institut de Robòtica i Informàtica Industrial (CSIC-UPC), Llorens i Artigas, 4-6, 08028 Barcelona, Spain;

<sup>2</sup> Suez Research Center, Nanjing West Road 800, Shanghai 40001, China;

<sup>3</sup> CETaqua, Water Technology Centre, Barcelona, 08904, Spain;

\* Correspondence: [csun@iri.upc.edu](mailto:csun@iri.upc.edu).

Benjami Parellada [<benjamiparellada@gmail.com>](mailto:benjamiparellada@gmail.com);

FENG Jing [<fengjing385@foxmail.com>](mailto:fengjing385@foxmail.com);

Vicenc Puig Cayuela [<vicenc.puig@upc.edu>](mailto:vicenc.puig@upc.edu);

Gabriela Cembrano [<gabriela.cembrano@upc.edu>](mailto:gabriela.cembrano@upc.edu).

**Abstract:** Pollution caused by combined sewer overflows has become a global threat to the environment. Under this challenge, quality-based real-time control (RTC) is considered as an effective approach to minimize pollution through generating optimal operation strategies for the sewer infrastructure. To suit the fast computation requirement of RTC implementation, simplified quality models are required. However, due to the hydrological complexity, it is not easy to develop simplified quality models which are amenable to be used in real-time computations. Under this context, this paper contributes 1) a preliminary analysis of influencing factors for the quality models of sewer networks in order to give supportive knowledge for both model developing and applying. Conceptual quality models which were proposed previously by the authors, with total suspended solid (TSS) as quality indicator, are used in this study. 2) Clustering algorithm is used for exploratory analysis. Further analysis about the correlations between different factors and model performance is also carried out. 3) All the study and analysis are demonstrated on a real pilot based on Louis Fargue urban catchment in Bordeaux. Conclusive results about the influencing factors, flow rate, rain intensity and pipe length, as well as their correlations with the TSS models are elaborated.

**Keywords:** analysis, influencing factor, quality model, real-time control, total suspended solid

---

## INTRODUCTION

In nowadays urban cities, combined sewer networks (SN) collect stormwater together with the wastewater and then send them to the wastewater treatment plants (WWTP) for purifying before releasing them into the receiving bodies (García *et al.* 2015). In storm weather, when the capacities of SN and the WWTP are overloaded, combined sewer overflow (CSO) occurs and generates harmful pollution to the environment (Butler & Schütze 2005; Becouze *et al.* 2009; Gasperi *et al.* 2008; Joseph-Duran *et al.* 2014). In order to provide proper service to the urban life, as well as to protect the water ecosystem, efficient management of SN through advanced control techniques is required.

In view of the recent advances in information and communications technology, real-time control (RTC) has been considered as an effective solution for the SN management due to the obvious advantages comparing with the traditional solutions of constructing infrastructure (Beeneken *et al.* 2013; Cembrano *et al.* 2004; Döring 1989; Dirckx *et al.* 2011; EPA 2006; Fanlin *et al.* 2017; Joseph-Duran *et al.* 2015; Puig *et al.* 2009; Schütze *et al.* 2004). Moreover, the integrated pollution-based RTC can generate system-wide effective strategies to reduce CSO volume, as well as the released pollution, through integrating the SN and WWTP considering both the quantity and quality measurements

46 (Fanlin *et al.* 2017; Sun *et al.* in press). This is also the main goal of the European project LIFE  
47 EFFIDRAIN (Efficient Integrated Real-time Control in Urban Drainage and Wastewater Treatment  
48 Plants for Environmental Protection) [Joseph-Duran *et al.* (2014, 2015); Ocampo-Martínez *et al.* 2013;  
49 Puig *et al.* 2009; Pleau *et al.* 2010; Schütze *et al.* 2004; Sun *et al.* (2017a, 2018a, b)].

50 There are plenty of physical models to describe quality dynamics in SN in detail, like the KUL  
51 Model (Combes 1982), Velikanov Model (van Rijn 1984) and Ackers White Model (Ackers & White  
52 1973). Moreover, simulation platforms which elaborate the hydrological dynamics through  
53 embedding quality equations are also available, the popular ones are SWMM (Huber 1988; Rossman  
54 2015), WaterCress (Clark 2002), Simba# (IFAK 2005), MIKE Urban (DHI 2007) and InfoWorks CS  
55 (MWH 2010). These high-fidelity models have sufficient capacities of representing quality dynamics  
56 accurately but need large computational effort and hard to be used into the RTC optimization. In  
57 order to take quality and its dynamics into RTC of urban drainage systems, simplified conceptual  
58 quality models must be used (Cembrano *et al.* 2004; Sun *et al.* in press). Taking into account the  
59 hydrological complexities of SN and the high data requirements for the model calibration, it is still a  
60 challenge to develop and apply conceptual quality models successfully.

61 To reduce the limitations of high-fidelity models and tools, new quality modelling approaches  
62 are proposed focused on total suspended solid (TSS) (see Vezzano *et al.* 2014), Chemical Oxygen  
63 Demand (COD) and ammonia (see Fu *et al.* 2010; Lacour & Schütze 2011). Besides, Vezzano *et al.* (2020)  
64 has also proposed just recently an online forecasting model and the performance evaluation of  
65 ammonium concentrations at the WWTP inlets. These modelling approaches were used to minimize  
66 the pollution loads from SN and WWTP inlets through including water quality into dynamic cost  
67 functions or prioritizing the CSO loads considering the recipient status (Fu *et al.* 2010; IFAK 2005;  
68 Lacour & Schütze 2011; Torres-Matallana *et al.* 2018; Vezzano *et al.* 2014). However, these quality  
69 models cannot be mapped inside the SN and cannot be used into the optimization process directly,  
70 either. Afterwards, (Sun *et al.* 2017b) proposed conceptual quality models for the SN, with TSS as the  
71 quality indicator, which demonstrate how the TSS can be mapped inside the sewers and be involved  
72 into the control process directly. However, the development and application of the quality models  
73 are greatly affected by the topology of the SN, the climate and the physical characteristics of the pilot.  
74 What are the influencing factors and how they correlated with performance of the quality models are  
75 still unknown and are important to be investigated.

76 Under this context, this paper contributes: 1) a preliminary analysis of the influencing factors for  
77 quality models in order to provide supportive guidelines for conceptual quality modelling and their  
78 further application at different pilots. In particular, the simplified TSS models proposed previously  
79 by the authors are used for analysis. Three possible factors rain intensity, sewer length, and flow rate  
80 are supposed very likely to affect the model performance. 2) To benefit from the new insight brought  
81 by the data processing techniques, clustering algorithm is used as the tool for grouping model  
82 performances and exploratory analyzing the influencing factors in this study. Afterwards, further  
83 analysis considering correlations between different influencing factors and the model performance is  
84 also carried out. The hydraulic and hydrology datasets for model calibration and validation, as well  
85 as the afterwards analysis, is produced through virtual reality simulations by EPA-SWMM5. 3) A real  
86 pilot based on the Louis Fargue urban catchment in Bordeaux (France) is used as case study.  
87 Conclusive results about the influencing factors (flow rate, rain intensity and pipe length) as well as  
88 their correlations with performance of the TSS models are provided afterwards.

## 89 MATERIALS AND METHODS

### 90 Conceptual TSS models

91 Physically, the TSS dynamics inside a sewer include solids transportation, sedimentation and  
92 erosions, which are easily affected by the hydraulic parameters. Three different conceptual models  
93 have been proposed in (Sun *et al.* 2017b). These simplified TSS models are analysed in this paper,  
94 whose model equations are briefly presented as:

95 Model 1

$$96 \quad \mathbf{ss}_{out}(k+1) = (1 - \alpha)\mathbf{ss}_{out}(k) + \alpha\mathbf{ss}_{in}(k) \quad (1)$$

97 Model 2

$$98 \quad \mathbf{ss}_{out}(k+1) = \alpha_1\mathbf{ss}_{out}(k) + \alpha_2\mathbf{ss}_{in}(k) \quad (2)$$

99 Model 3

$$100 \quad \mathbf{ss}_{out}(k+1) = \beta\mathbf{ss}_{in}(k-d) + e \quad (3)$$

101 where  $\mathbf{ss}_{out} \in \mathbb{R}^{n_s}$  and  $\mathbf{ss}_{in} \in \mathbb{R}^{n_s}$  represent the output and input vectors of TSS concentrations [mg/l] for the sewers, respectively;  $k \in \mathbb{N}^+$  is the current time step;  $d \in \mathbb{N}^+$  represents the TSS transportation delay;  $\alpha, \alpha_1, \alpha_2, \beta, d, e$  are the model coefficients which need to be calibrated for each sewer under different rain scenarios while  $n_s$  is the maximal number of sewers.

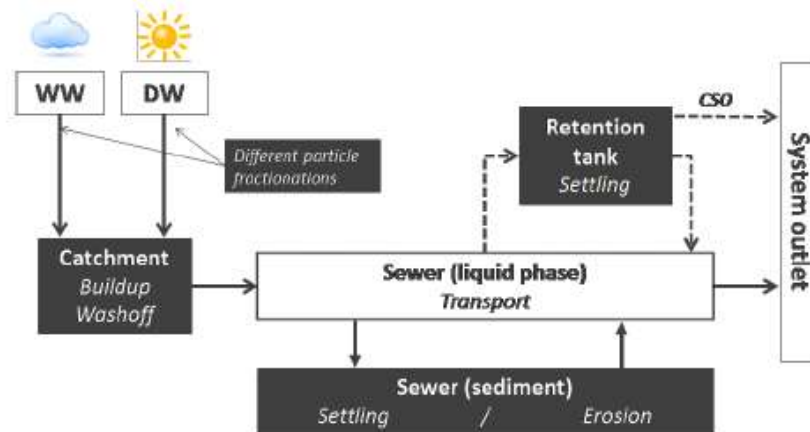
102  
103  
104  
105 In order to analyse these simplified TSS models, the flow rate, rain intensity and sewer length are considered as the three most relevant hydraulic factors which are likely to affect the model performance.  
106  
107

## 108 Analysis tools

109 Before performance analysing, the conceptual TSS models presented in the previous section are firstly calibrated and validated using datasets generated through virtual reality simulations under different scenarios. The hydraulic datasets are produced by the simulator EPA-SWMM5. The quality data is generated through the library SWMM-TSS (Maruėjouls *et al.* 2012) from LyRE (R+D centre of Suez) based on extended Barre de Saint Venant equation set in SWMM5, which can reproduce the TSS transport, sediment accumulation and erosion in sewers and retention tanks (Wiuuff 1985).  
110  
111  
112  
113  
114

115 Figure 1 illustrates modifications made by SWMM-TSS in the SWMM5 library model, where the boxes correspond to the existing modules in SWMM5 while grey boxes are the ones added for representing the quality module. The abbreviations WW and DW represent the wet and dry weather respectively.  
116  
117  
118

119 Besides the SWMM5 simulator, MATLAB and GAMS optimization software (Richard 2016) are also used in the calibration process. RStudio, which is an open source software for R (Krotov 2017), is used for grouping and analysing the model performances through clustering algorithm.  
120  
121



122  
123 **Figure 1.** Structure of Quality Module SWMM-TSS  
124

125 The Nash Sutcliffe model efficiency coefficient (NSE) (Nash & Sutcliffe 1970) is used to describe calibration performance of the TSS models:  
126

$$127 \quad fit_{i,j}^m = 1 - \frac{\sum_{k=1}^K (ss_{out}^{i,j,m}(k) - \hat{ss}_{out}^{i,j,m}(k))^2}{\sum_{k=1}^K (\hat{ss}_{out}^{i,j,m}(k) - \overline{\hat{ss}_{out}^{i,j,m}})^2} \quad (4)$$

128 where  $ss_{out}^{i,j,m}$  is the predicted TSS value using the model  $m$  ( $m \in [1,2,3]$ ) for the sewer  $i$  under the rain scenario  $j$ ,  $\hat{ss}_{out}^{i,j,m}$  is the corresponding TSS value read from the simulator and  $\overline{\hat{ss}_{out}^{i,j,m}}$  is average of it,  $K \in \mathbb{N}^+$  represents maximal number of time steps in one rain scenario. The fitting performance  $fit \in \mathbb{R}^{n_s \times n_r \times 3}$  can range from  $-\infty$  to 1 ( $n_r$  represents maximal number of rain scenarios used for analysis). The higher it is; the better performance the model has.  
129  
130  
131  
132

## 133 Data structure

134 After the calibration process, enough data are generated to structure the matrix  $D \in \mathbb{R}^{(n_s * n_r * 3)}$  to be  
 135 used for the performance analyzing. The matrix  $D$  includes fitting performance vector  $\mathbf{fit} \in$   
 136  $\mathbb{R}^{n_s * n_r * 3}$ , the corresponding flow rate vector  $\mathbf{flow} \in \mathbb{R}^{n_s}$  [l/s], sewer lengths  $\mathbf{len} \in \mathbb{R}^{n_s}$  [m], as well  
 137 as the rain intensities  $\mathbf{rain} \in \mathbb{R}^{n_r}$  [mm]. The format of matrix  $D$  is presented as:  
 138

$$139 \quad D = \begin{bmatrix} fit_{1,1}^1 & flow_1 & rain_1 & len_1 \\ fit_{2,1}^1 & flow_2 & rain_1 & len_2 \\ \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ fit_{n_s, n_r}^3 & flow_{n_s} & rain_{n_r} & len_{n_s} \end{bmatrix}$$

## 140 Clustering algorithm

141 A clustering algorithm (Rodriguez & Laio 2014; Soldevila *et al.* 2016) is used for the exploratory  
 142 analysis of model performances based on the matrix  $D$ , which includes all the influencing features to  
 143 be analyzed. Considering the given matrix, clustering algorithm can return a list of  $c$  clusters  $C =$   
 144  $\{c_1, \dots, c_c\}$ . To achieve this, firstly, each data point is assigned a measurement grade  $G = g_{i,j} \in$   
 145  $[0,1], i = 1, \dots, (n_s * n_r * 3), j = 1, \dots, c$ , to indicate its possibility belongs to each of the cluster. And  
 146 after that, the clustering process is proceeded through minimizing the following objective function:

$$147 \quad \arg \min_c \sum_{i=1}^{n_s * n_r * 3} \sum_{j=1}^c g_{i,j}^\alpha \|x_i - c_j\|^2 \quad (5)$$

148 where  $x \in \mathbb{R}^{n_s * n_r * 3}$  is the data point being analysed;  $\alpha$  is a fuzzy number to determine level of  
 149 cluster fuzziness. To have a crisp partitioning in this case,  $\alpha$  is put 1, and at that time, the  
 150 measurement grade is converge to 0 or 1.

151 In this study, the three proposed TSS models are analysed firstly to conclude which model works  
 152 best through clustering their fitting performance  $\mathbf{fit}$ . Under this objective, the number of returned  
 153 clusters  $c$  is set as 3; the data point vector being analysed  $x$  is set as  $\mathbf{fit}$ ;  $m$  is 1; and the  
 154 measurement grade  $g_{i,j}^m$  for the  $m$ -th cluster under the  $j$ -th rain scenario is computed for all the sewers  
 155  $\forall i \in 1, \dots, n_s$  using the following equation:

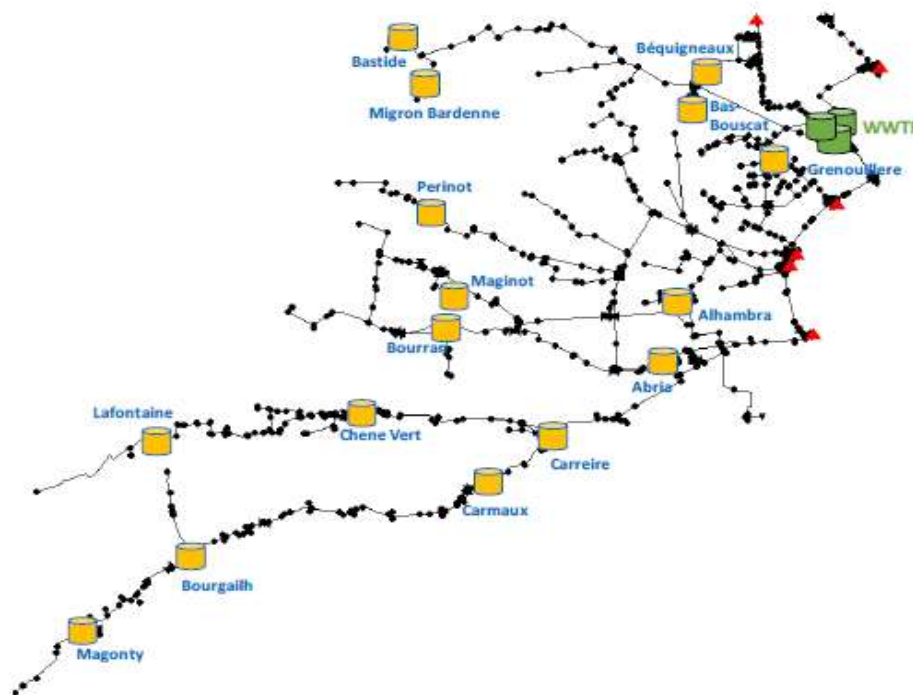
$$156 \quad g_{i,j}^m = \begin{cases} 0, & fit_{i,j}^m < \max_{m \in C} fit_{i,j}^m \\ 1, & fit_{i,j}^m = \max_{m \in C} fit_{i,j}^m \end{cases} \quad (6)$$

157 The cluster which has maximal data points is concluded as the best performance model.

## 158 CASE STUDY

### 159 Louis Fargue Catchment

160 The Louis Fargue catchment is the most populated catchment in the Bordeaux Metropole, which has  
 161 an area of around 7,700 ha and accommodate about 300,000 inhabitants. Figure 2 is a layout of this  
 162 network in SWMM. The total sewer network length of Louis Fargue catchment is 1,340km with 80%  
 163 combined while 20% separated. Most of these pipes have a circular shape with diameters ranging  
 164 from 300 mm to 4500 mm. In the dry weather, the wastewater is collected and transferred all the way  
 165 to the sub-catchment outlets (connections represented by red triangles in Figure 2) where it is then  
 166 carried to the WWTP through a large interceptor. At each connection point (an outlet), there is a  
 167 combined sewer overflow structure to discharge excessive combined water into the Garonne river  
 168 during storm weather. All these descriptions are referred from (Ly 2019), where reader is referred to  
 169 obtain more details about this catchment.  
 170



171

172 **Figure 2.** Louis Fargue Catchment in SWMM referred in (Ly 2019)

173 Rain scenarios for calibration and validation come from the real rainfall measured at Bordeaux  
 174 in the year of 2016. The 129 hour raining data since 01/30/2016 is used for calibration, which  
 175 corresponds to 14 different rain events according to their sub-catchment districts (Perinot,  
 176 LaFontaine, Carreire, etc.).

### 177 Exploratory Analysis

178 In order to focus on analysing the sewer model, all the conduits in Louis Fargue catchment are  
 179 recompiled. The conduits with one entrance and one exit are filtered for analysing, and there are in  
 180 total 122 conduits. The corresponding rainfall measurements is assigned to each conduit by checking  
 181 the sub-catchment it belongs to. Virtual reality simulation based on SWMM and SWMM-TSS is  
 182 applied in a certain time period of 129 hours to generate hydraulic and hydrology datasets for the  
 183 following calibration processes. Afterwards, all of these 122 sewers are calibrated for the three models  
 184 through MATLAB and GAMS codes. Calibration and model performance results are obtained for the  
 185 122 sewers with the three models. All the sequential values from each of the simulations is then used  
 186 to construct the Matrix  $D$ , where a total of 5124 feature vectors are analysed for the 122 different  
 187 conduits under 14 different rain events with 3 TSS models.

188 The clustering algorithm is applied firstly to generate the measurement grade  $g_{i,j}^m$  to check for  
 189 each conduit which of the three models is the best. The results are presented in Table 1 showing the  
 190 times each model presents best performance for the 122 conduits.

191 **Table 1** Exploratory Analysis Results

	Model 1	Model 2	Model 3
grade	13	1534	161

192 Table 1 shows that Model 1 is not working as well as the other two, whose measurement grade  
 193 is 13, the minimal one among the three models. Only few conduits are found with performance  
 194 evaluation higher than both of the Model 2 and Model 3. However, even though for the 13 scenarios  
 195 when the Model 1 works better than the others two, it does not mean it is a better model. Table 2  
 196 shows in detail for the scenarios when Model 1 works better, which indicates that the fitting

197 performances of Model 1 do not behave so well, either. Furthermore, it can also be seen that it is  
 198 always the same conduits which provoke this deterioration in the other two models (all the names of  
 199 the conduits are created due to confidential requirements of the pilot).

200 **Table 2** Scenarios work best for Model 1

Scenarios	<i>fit</i> <sup>1</sup>	<i>fit</i> <sup>2</sup>	<i>fit</i> <sup>3</sup>	From conduit	To conduit
$S_1^1$	0.000	-0.038	-0.084	Link_P_95_1	Link_BV_1
$S_2^1$	0.024	-0.114	-0.260	Link_P_95_1	Link_BV_1
$S_3^1$	0.359	0.027	-0.180	Link_EN_1	Link_905_1
$S_4^1$	0.000	-0.211	-11.10	Link_P_95_1	Link_BV_1
$S_5^1$	0.000	-2.940	-1.781	Link_G14_1	Link_G19_1
$S_6^1$	0.000	-0.085	-4.102	Link_P_95_1	Link_BV_1
$S_7^1$	0.074	0.055	0.036	Link_EN_1	Link_905_1
$S_8^1$	0.000	-0.066	-21.937	Link_P_95_1	Link_BV_1
$S_9^1$	0.000	-9.651	-5.681	Link_255_1	Link_260_1
$S_{10}^1$	0.000	-0.220	-4.657	Link_P_95_1	Link_BV_1
$S_{11}^1$	0.002	-3.713	-0.642	Link_BO_1	Link_AC_1
$S_{12}^1$	0.082	-1.176	-0.640	Link_G14_1	Link_G19_1
$S_{13}^1$	0.000	-0.004	-7.059	Link_P_95_1	Link_BV_1

201 Both Model 3 and Model 2 are good in the average case with higher measurement grades. The  
 202 mean fitting value for Model 1 is 0.7787036 and for model 2 is 0.8009895. When comparing Model 2  
 203 and Model 3, it is clear that Model 2 performs better. Moreover, for Model 3, some poor results  
 204 (negative fitting performances) have been obtained as illustrated in Table 3:

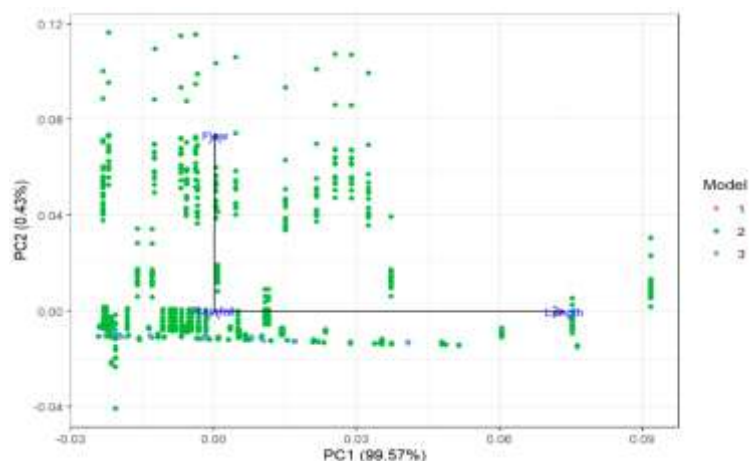
205 **Table 3** Example scenarios work worst for Model 3

Scenarios	<i>fit</i> <sup>1</sup>	<i>fit</i> <sup>2</sup>	<i>fit</i> <sup>3</sup>	From conduit	To conduit
$S_1^3$	0.000	0.191	-1.833	Link_OR1_1	Link_OR2_2
$S_2^3$	0.000	0.441	-8.106	Link_OR1_1	Link_OR2_2
$S_3^3$	0.000	0.594	-6.521	Link_OR1_1	Link_OR2_2
$S_4^3$	0.000	0.534	-6.405	Link_OR1_1	Link_OR2_2
$S_5^3$	0.002	0.003	-2.526	Link_OR1_1	Link_OR2_2
$S_6^3$	0.000	0.016	-5.399	Link_OR1_1	Link_OR2_2
$S_7^3$	0.000	0.016	-2.215	Link_OR1_1	Link_OR2_2
$S_8^3$	0.000	-0.066	-2.194	Link_P_95_1	Link_BV_1
$S_9^3$	0.000	0.768	-2.098	Link_AA_3	Link_PG_1

206  
 207 From Table 3, it is clear that the conduit from Link\_OR1\_1 to Link\_OR2\_2 is not represented  
 208 particularly well. Among these first results, it can be concluded that Model 2, in most scenarios, works  
 209 better with an average fitting performance of 89.81%, which takes into account mostly the physical  
 210 processes with sufficient calibration space.

211 After grouping the best performance model (Model 2) through clustering algorithm, a principle  
 212 component analyses (PCA) is carried out to initially evaluate influence of the three possible factors  
 213 (principle components) flow rate, length and rainfall to the performance of the quality models. As

214 shown in the Figure 3, where the different axis represents a linear combination for the three features,  
 215 flow rate, length and rainfall from the available dataset. All the points are the centroids of each of the  
 216 different individual data (e.g. for one simulation the conduit that goes from *linkX* to *linkY* is  
 217 represented by a point on the plot). The objective of this PCA is to see which feature influence more  
 218 of the performance. And it is clear to conclude that sewer length is the most influential feature for  
 219 these TSS models, since it captures almost all of the variability of the dataset (99.57%). While rainfall  
 220 is not very well represented in this case study based on the current simulations, and it is still hard to  
 221 arrive to a final conclusion. Studying the other principal components, it is difficult either to separate  
 222 which model works best for the three given features. In order to arrive more clear conclusion, further  
 223 exploratory analysis is applied to search more correlations between the factors and the model  
 224 performances.

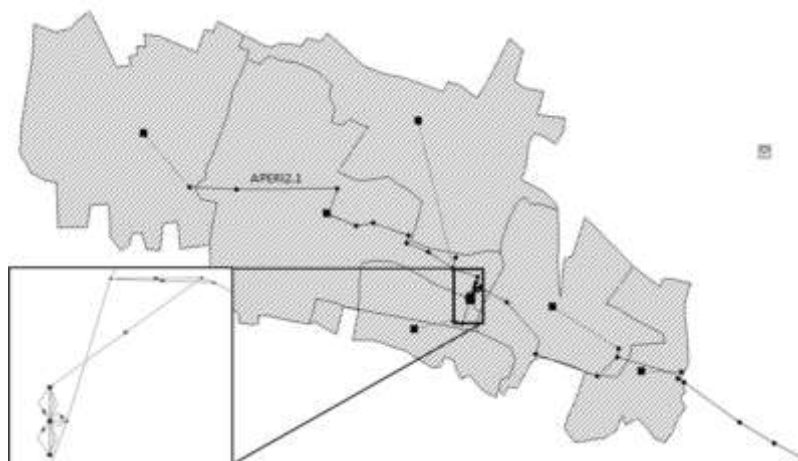


225  
 226 **Figure 3.** PCA for the influencing features

### 227 Correlation Exploratory Analysis

228 In order to explore further the correlation between each factor and the model performances, one of  
 229 the sub-catchments of Luis Fargue catchment, the Perinot SN (Figure 4) with additional simulations  
 230 under more representative rainfalls is applied.

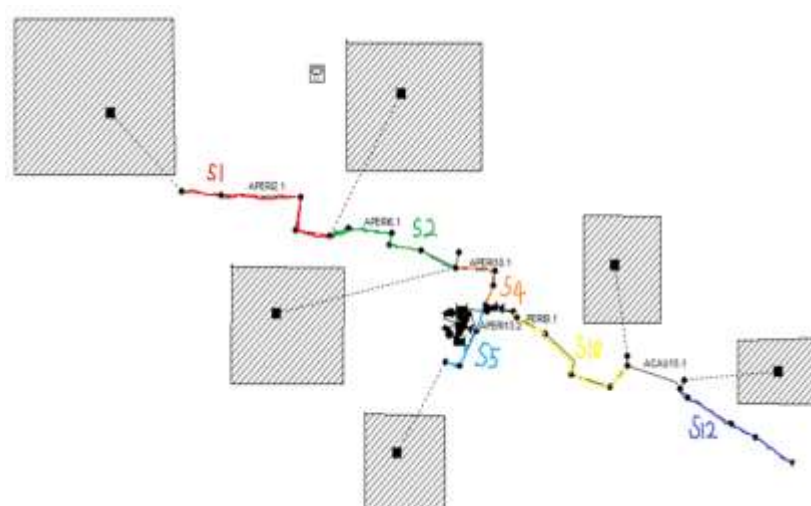
231 The Perinot SN covers a total area of 260 ha with mainly residential uses. The sewer length for  
 232 the Perinot SN is 3 km with an average slope of 0.007. A retention tank which is separated in three  
 233 hydraulically connected bodies for a total storage volume of 35000 m<sup>3</sup> is also included. In order to  
 234 simplify the tests and control afterward, sewers of similar dynamics in series are integrated as one,  
 235 where five main sewers are presented (Figure 5).



236

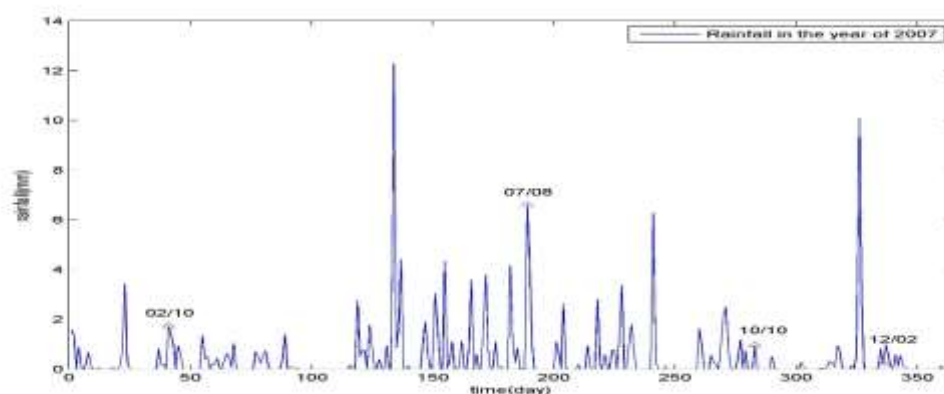


237 **Figure 4.** Detail topology of the Perinot sub-catchment



238  
239 **Figure 5.** Perinot SN after pre-treatment

240 In order to consider a set of rain scenarios more representative of the rain intensities, rain  
241 scenarios for calibration and validation of the Perinot SN corresponding to real rainfall measured at  
242 France in the years 2003, 2007, 2011 and 2013. Besides, four different scenarios with various  
243 characteristics (Table 4) have been selected from historic data of 2007 (Figure 6), which represent  
244 different types of rainfalls with the 5-minute time step and 24 hours' duration.  
245



246  
247 **Figure 6.** Rain Scenario of Perinot in the year of 2007

248 **Table 4** Different rainfall scenarios

	1	2	3	4
Start time	Oct/10/2007	Dec/02/2007	Feb/10/2007	Jul/08/2007
	5	6	7	8
Start time	Aug/19/2003	Aug/02/2013	Jan/03/2011	Jan/03/2011
Duration	24h		<b>Time step</b>	5 min

249  
250 The calibration process is also carried out using SWMM5 embedded with SWMM-TSS, Matlab  
251 and the GAMS optimization library. Table 5 provides more details about the arrangement about the  
252 rain scenarios, where the rain scenarios 1, 2, 5 and 7 will be used for calibration. After calibrating all  
253 the models, rain scenarios 3, 4, 6 and 8 will be used for validating the calibrated models.



254

**Table 5** Test Arrangement

Rain	Calibration	Case1		Case2		Case3		Case4	
	Validation	3	4	3	4	6	8	6	8
Sewer	$S_i$	$S_i - 1$		$S_i - 2$		$S_i - 5$		$S_i - 7$	
		$S_i - 1 - 3$		$S_i - 2 - 3$		$S_i - 5 - 6$		$S_i - 7 - 6$	
		$S_i - 1 - 4$		$S_i - 2 - 4$		$S_i - 5 - 8$		$S_i - 7 - 8$	

255

$S_i$  includes S1, S2, S4, S5, S10, S12; xx-xx-xx means sewer-calibration-validation

256

Correlation between sewer length and model performance

257

After the model calibration and validation, Table 6 and Figure 7 present the correlation relations between sewer length and the model performance. It seems that all three models present a similar tendency changing the sewer lengths. However, the performance of Model 3 changes more dramatically than Models 1 and 2. Table 7 shows how sewer length affects the coefficient parameters of Model 3. Sewer 5 and 10 perform worse with lower value of  $\beta$  but much higher  $e$ . Model 3 is generalized from the physical characteristics in a sewer, where the TSS dynamic is affected by the flow rate and time delays, which are affected directly by sewer length. Therefore, it can be concluded that up to some extent, the length of sewer has more impact on the performance of Model 3.

258

259

260

261

262

263

264

265

In conclusion, the length of sewer is more likely to influence the performance of Model 3. But in general, Model 1 and 2 seem to be good choices for sewers which length ranges from 400m to 900m.

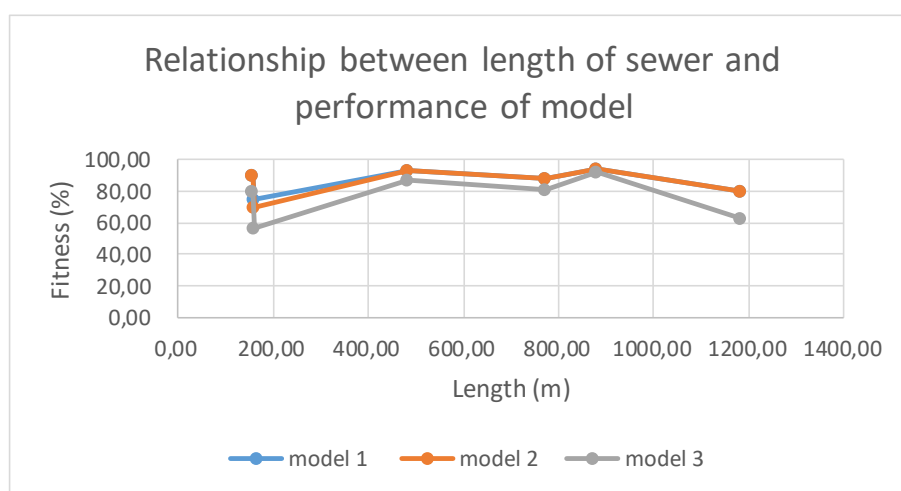
266

267

**Table 6** Relationship between sewer length and model performance

Sewer	Length (m)	Model 1 (%)	Model 2 (%)	Model 3 (%)
S4	156.20	90.31	90.45	80.37
S5	160.70	75.09	69.43	56.82
S2	482.60	93.10	93.12	86.61
S10	773.40	87.73	87.70	81.30
S12	879.20	94.02	94.09	92.46
S1	1181.90	79.53	79.91	62.63

268



269

270

**Figure 7.** Relationship between sewer length and model performance

271

**Table 7** Relationship between sewer length and Model 3 parameters

Sewer	Length (m)	$\beta$	$e$	Model 3 (%)
S4	156.20	0.96	10.35	80.37
S5	160.70	0.71	47.53	56.82

<b>S2</b>	482.60	0.97	9.65	86.61
<b>S10</b>	773.40	0.95	19.02	81.30
<b>S12</b>	879.20	0.97	11.74	92.46
<b>S1</b>	1181.90	0.73	86.04	62.63

## 272 Correlation between rainfalls and model performance

273 Table 9 illustrates correlation between rain intensity and model performances. As in Table 8,  
 274 rainfall scenarios 1 and 2 can be regarded as light rain, while scenario 5 and 7 correspond to heavy  
 275 rain. It seems that, with the increase of rainfall intensity,  $a$  decreases for Model 1;  $a_1$  increases while  
 276  $a_2$  decreases for Model 2;  $\beta$  decreases while  $e$  increases for Model 3. Overall, there is a tendency  
 277 that the heavier rainfall is, the worse model performance will be obtained.

278 **Table 8** Information of rainfall scenarios in calibration

Rainfall for Calibration	Total Depth of 24h(mm)	Intensity(mm/ h)	Maximum Depth (mm)
<b>1</b>	5.53	0.23	0.04
<b>2</b>	0.25	0.01	0.06
<b>5</b>	1754.61	73.11	19.05
<b>7</b>	1667.78	69.49	45.71

279

280 **Table 9** Relationship between rain intensity and model performance in calibration

Scenario	$a$	$a_1$	$a_2$	$\beta$	$e$	Model 1(%)	Model 2 (%)	Model 3 (%)
<b>case 1</b>	0.47	0.48	0.47	0.89	15.66	92.79	92.87	80.98
<b>case 2</b>	0.46	0.54	0.46	0.92	21.07	92.30	92.36	78.17
<b>case 3</b>	0.35	0.65	0.35	0.88	36.30	88.78	91.16	71.71
<b>case 4</b>	0.42	0.58	0.42	0.84	49.86	80.35	81.62	67.25

## 281 Correlation between flow rate and model performance

282 Figure 8 shows the relationship between flow rate and TSS out of a sewer. Although there is no  
 283 distinct evidence of the relationship between these two variables, we can still find that the trend of  
 284 discharge is likely to be opposite against the trend of concentration of TSS in a sewer. This can be  
 285 understood that the flow with large velocity will take away more TSS, thereby the concentration of  
 286 TSS decreasing.

287 In SWMM, the manning equation is used to express the relationship between flow rate, slope,  
 288 cross-sectional area and hydraulic radius in conduits. It shows that, the flow rate in a sewer is affected  
 289 by many different parameters and physical characteristics of the conduit. However, how they affect  
 290 the flow rate, and how they cross correlated among different parameters require further study in  
 291 future. On another hand, flow rate and TSS are normally considered as the main variables to integrate  
 292 SN and WWTP. In order to have a better integrated management of SN and WWTP, what is the  
 293 underlying relationship between TSS and flow rate, as well as other potential parameters (i.e. slope,  
 294 diameter) will be investigated as the next step.

295

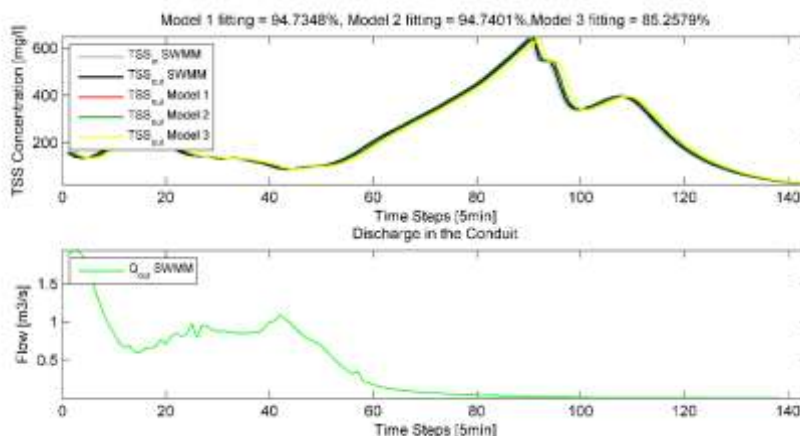


Figure 8. Flow rate and TSS behavior out of Sewer 1

296

297

## 298 CONCLUSIONS

299 This paper contributes a preliminary analysis of the influencing factors for the performance of SN  
 300 quality models. In particular, a set of conceptual TSS models proposed previously are used for this  
 301 study. Three possible factors rain intensity, sewer length, and flow rate are analysed through a series  
 302 of tests. A clustering algorithm is used to explore preliminary the best performance model. Further  
 303 exploratory analysis is carried out afterwards to obtain correlations between different influencing  
 304 factors and the model performance. This study also contributes potentially to a better quality-based  
 305 RTC management of SN and WWTP, which can lead to improvements in CSO and pollution  
 306 reduction to the water environment.

307 Through this study, the following conclusive results are obtained:

- 308 1) Preliminary analysis shows that Model 2 and Model 3 perform better than Model 1. After  
 309 comparing the Model 2 and Model 3, Model 2 shows better performance in more scenarios  
 310 with an average fitting performance of 80.10%. On the other hand, PCA analysis concludes  
 311 that the sewer length is the factor which can influence the performance most;
- 312 2) Further exploratory analysis illustrates that the sewer length is more likely to influence Model  
 313 3. Models 1 and 2 are good choices for sewers with length ranges from 400m to 900m. Also,  
 314 there is a tendency that the heavier rainfall is, the worse model performance will be obtained.
- 315 3) From the further exploratory analysis, it may also be concluded that it is better to have larger  
 316 parameters  $a$ ,  $a_2$ ,  $\beta$  and smaller  $a_2$ ,  $e$  for the models to perform better when there is lack of  
 317 rainfall data for calibration. Besides, the trend of discharge is likely to be opposite to the trend  
 318 of TSS in a sewer, which can be explained because the flow rate with large velocity takes away  
 319 more TSS.
- 320 4) More conclusive results were in expectations which can indicate clearer usability of the  
 321 models in RTC, when specific parameter sets can be used directly; when re-calibrations are  
 322 required, etc. However, the current analysis based on the available pilots did not provide  
 323 enough evidences to support these conclusions. Therefore, further analysis is still required.
- 324 5) Cross correlation between model performance and the potential influencing factors sewer  
 325 slope, diameters and velocity will also be investigated as the next step.

## 326 Acknowledgement

327 The authors wish to thank the support received by the European Commission research grant of  
 328 project LIFE EFFIDRAIN (LIFE14 ENV/ES/000860), thank the support from Spanish national project  
 329 DEOCS (DPI2016-76493-C3-3-R). The authors also want to thank Bordeaux Metropole and Aigües de  
 330 Barcelona for the financial and technical support. This work is also supported by the Spanish State  
 331 Research Agency through the María de Maeztu Seal of Excellence to IRI (MDM-2016-0656), by the  
 332 Institute of Robotics Industry through the TWINS project.

333 **References**

- 334 Ackers, P. & White, W. 1973 Sediment transport: a new approach and analysis. *J. Hydra. Divi.*, 99(11), 2041-2060.
- 335 Butler, D., & Schütze, M. 2005 Integrating simulation models with a view to optimal control of urban wastewater  
336 systems. *J. Environ. Modell. and Softw.*, 20(4), 415-426, 2005. [doi.org/10.1016/j.envsoft.2004.02.003](https://doi.org/10.1016/j.envsoft.2004.02.003)
- 337 Becouze, C., Bertrand-Krajewski, J. -L., Dembélé, A., Cren-Olivé, & Coquery, M. 2009 Preliminary assessment of  
338 fluxes of priority pollutants in stormwater discharges in two urban catchments in Lyon, France. *In: 13th of IWA*  
339 *intern. confer. on Diffuse Pollu. and Integ. Waters. Manage (DIPCON), Seoul/South Korea*, 12-15 October 2009.
- 340 Beeneken, T., Erbe V., Messmer, A., Reder, C., Rohlfing, R., Scheer, M., Schuetze, M., Schumacher, B., Weilandt,  
341 M. & Weyand, M. 2013 Real time control of urban drainage systems—a discussion of the additional efforts  
342 compared to conventionally operated systems. *Urban Water Journal*, 10(5), 293–299.  
343 [doi.org/10.1080/1573062X.2013.790980](https://doi.org/10.1080/1573062X.2013.790980)
- 344 Combes, V. 1982 *Etude de modèles mathématiques de transport des matériaux solides en réseau d'assainissement (Study*  
345 *of mathematical models of transport of solid materials in sewerage network)*. DEA de mécanique, Institut National  
346 Polytechnique, Toulouse, France.
- 347 Clark, R., Pezzaniti, D. & Cresswell, D. 2002 Watercress—Community Resource Evaluation and Simulation  
348 System—A tool for innovative urban water system planning and design. *In: Proceedings of the Hydrology and Water*  
349 *Resources Symposium, Melbourne/Australia*, 20–23 May 2002.
- 350 Cembrano, G., Quevedo, J., Salameo, M., Puig, V., Figueras, J., & Martí, J. 2004 Optimal control of urban  
351 drainage systems. A case study. *J. Contr. Engin. Pract.*, 12(1), 1-9. [doi.org/10.1016/S0967-0661\(02\)00280-0](https://doi.org/10.1016/S0967-0661(02)00280-0)
- 352 Döring, R. 1989 *Real-time control of urban drainage systems. The state-of-art*. IAWPRC, International Association on  
353 Water Pollution and Control, University of Michigan.
- 354 DHI. 2007 MIKE URBAN. <https://www.mikepoweredbydhi.com/products/mike-urban> (accessed 24 October  
355 2018)
- 356 Dirckx, G., Schütze, M., Kroll, S., Thoeys, C., De Gueldre, G. & Van De Steene, B. 2011 RTC versus static solutions  
357 to mitigate CSO's impact. *In: 12nd International Conference on Urban Drainage (ICUD)*, Porto Alegre/Brazil, 11-16  
358 September 2011.
- 359 Ly, D.K. 2019 *Water quality-based real time control of combined sewer systems*. PhD thesis, Environmental  
360 Engineering. Université de Lyon - INSA Lyon, France.
- 361 EPA. 2006 *Real time control of urban drainage networks*, Technical Report EPA/600/R-06/120, Environmental  
362 Protection Agency, Washington D.C., United States.
- 363 Fu, G., Khu, S., & Butler, D. 2010 Optimal distribution and control of storage tank to mitigate the impact of new  
364 developments on receiving water quality. *J. Environ. Engine.*, 136(3), 335-342. DOI: [10.1061/\(ASCE\)EE.1943-](https://doi.org/10.1061/(ASCE)EE.1943-7870.0000161)  
365 [7870.0000161](https://doi.org/10.1061/(ASCE)EE.1943-7870.0000161)
- 366 Fanlin M.; Guangtao F. & David B. 2017 Cost-effective river water quality management using integrated real-  
367 time control technology. *Environ. Sci. Technol.*, 51(17), 9876-9886. [doi.org/10.1021/acs.est.7b01727](https://doi.org/10.1021/acs.est.7b01727)
- 368 Gasperi, J., Garnaud, S., Rocher, V., & Moilleron, R. 2008 Priority pollutants in wastewater and combined sewer  
369 overflow. *J. Scien. of the Tot. Environ*, 407(1), 263-272. [doi.org/10.1016/j.scitotenv.2008.08.015](https://doi.org/10.1016/j.scitotenv.2008.08.015)
- 370 García, L., Barreiro-Gomez, J., Escobar, E., Téllez, D., Quijano, N., & Ocampo-Martínez, C. 2015 Modelling and  
371 real-time control of urban drainage systems: A review. *Advances in Water Resources*, 85, 120-132.  
372 [doi.org/10.1016/j.advwatres.2015.08.007](https://doi.org/10.1016/j.advwatres.2015.08.007)
- 373 Huber, W.C. & Dickinson, R.E. 1988 *Storm Water Management Model, User's Manual*, U.S. Environmental  
374 Protection Agency, Athens, GA, USA.

- 375 IFAK. 2005. SIMBA# 5.0 user's guide, <https://nextcloud.ifak.eu/s/simba3?path=%2FFlyer#pdfviewer> (accessed 1  
376 October 2019).
- 377 Joseph-Duran, B., Ocampo-Martínez, C., & Cembrano, G. 2014 Hybrid modelling and receding horizon control  
378 of sewer network. *Water Resources Research*, 50(11), 8497-8514. [doi.org/10.1002/2013WR015119](https://doi.org/10.1002/2013WR015119)
- 379 Joseph-Duran, B., Ocampo-Martínez, C., & Cembrano, G. 2015 Output-feedback control of combined sewer  
380 networks through receding horizon control with moving horizon estimation. *Water Resources Research*, 51(10),  
381 8129-8145. [doi.org/10.1002/2014WR016696](https://doi.org/10.1002/2014WR016696)
- 382 Krotov, V. 2017 *A Quick Introduction to R and RStudio*, Technical report. Murray State University, Murray,  
383 Kentucky. DOI: [10.13140/RG.2.2.10401.92009](https://doi.org/10.13140/RG.2.2.10401.92009).
- 384 Lacour, C., & Schütze, M. 2011 Real-time control of sewer systems using turbidity measurements. *Water Science  
385 & Technology*, 63(11), 2628-2632. [doi.org/10.2166/wst.2011.159](https://doi.org/10.2166/wst.2011.159)
- 386 MWH 2010. InfoWorks CS. [http://www.innovyze.com/products/infoworks\\_cs/](http://www.innovyze.com/products/infoworks_cs/) (accessed 24 October 2018)
- 387 Maruéjols, T., Vanrolleghem, P., Pelletier, G., & Lessard, P. 2012 A phenomenological retention tank model  
388 using settling velocity distributions. *J. Wat. Res.*, 46, 6857-6867. [doi.org/10.1016/j.watres.2011.11.067](https://doi.org/10.1016/j.watres.2011.11.067)
- 389 Nash, J.E. & Sutcliffe, J.V. 1970 River flow forecasting through conceptual models part I-A discussion of  
390 principles. *Journal of Hydrology*, 10(3), 282-290. [doi.org/10.1016/0022-1694\(70\)90255-6](https://doi.org/10.1016/0022-1694(70)90255-6)
- 391 Ocampo-Martínez, C., Puig, V., Cembrano, G. & Quevedo, J. 2013 Application of predictive control strategies to  
392 the management of complex networks in the urban water cycle [applications of control]. *IEEE Control Systems*,  
393 33(1), 15-41. DOI: [10.1109/MCS.2012.2225919](https://doi.org/10.1109/MCS.2012.2225919)
- 394 Puig, V., Cembrano, G., Romera, J., Quevedo, J., Aznar, B. R., & Cabot, J. 2009 Predictive optimal control of sewer  
395 networks using CORAL tool: application to Riera Blanca Catchment in Barcelona. *Water science & Technology*,  
396 60(4), 869-878. [doi.org/10.2166/wst.2009.424](https://doi.org/10.2166/wst.2009.424)
- 397 Pleau, M., Fradet, O., Colas, H. & Marcoux, C. 2010 Giving the rivers back to the public. Ten years of real time  
398 control in quebec city. In: *International Conference on Sustainable Techniques and Strategies for Urban Water  
399 Management (NOVETECH)*, Lyon/France, 28-30 June 2010.
- 400 Rodriguez, A. & Laio, A. 2014 Clustering by fast search and find of density peaks. *Science*, 344 (6191), 1492-1496.  
401 DOI: [10.1126/science.1242072](https://doi.org/10.1126/science.1242072)
- 402 Rossman, L. 2015 *Storm Water Management Model*, Users' Manual Version 5.1, *Envir. Prot. Agn*, Washington D.C.,  
403 USA.
- 404 Richard, E. 2016 *GAMS - A Users' Guide*. Washington, DC, USA.
- 405 Schütze, M., Campisano, A.C., Colas, H., Schilling, W. & Vanrolleghem, P.A. 2004 Real time control of urban  
406 wastewater systems - where do we stand today? *J. Hydro.*, 299(3-4), 335-348. [doi.org/10.1016/j.jhydrol.2004.08.010](https://doi.org/10.1016/j.jhydrol.2004.08.010)
- 407 Soldevila, A., Blesa, J., Tornil-Sin, S., Duviella, E., Fernandez-Cantí, R.M. & Puig, V. 2016 Leak localization in  
408 water distribution networks using a mixed model-based/data-driven approach. *Control Engineering Practice*, 55,  
409 162-173. [doi.org/10.1016/j.conengprac.2016.07.006](https://doi.org/10.1016/j.conengprac.2016.07.006)
- 410 Sun, C.C., Joseph, B., Maruejols, T., Cembrano, G., Muñoz, E., Meseguer, J., Montserrat, A., Sampe, S., Puig, V.  
411 & Litrico, X. 2017a Efficient integrated model predictive control of urban drainage systems using simplified  
412 conceptual quality models. In: *14th IWA/IAHR International Conference on Urban Drainage (ICUD)*, Prague/Czech,  
413 10-15 September 2017.
- 414 Sun, C.C., Joseph-Duran, B., Maruejols, T., Cembrano, G., Meseguer, J., Puig, V., & Litrico, X. 2017b Real-time  
415 control-oriented quality modelling in combined urban drainage networks. In: *IFAC 2017 World Congress*,  
416 *Toulouse/France*, 9-14 July 2017.

- 417 Sun, C.C., Cembrano, G., Puig, V. & Meseguer, J. 2018a Cyber-physical systems for real-time management in the  
418 urban water cycle. *In: 4th International Workshop on Cyber-Physical Systems for Smart Water Networks, Porto/Portugal,*  
419 10 April 2018.
- 420 Sun, C.C., Joseph, B., Cembrano, G., Puig, V. & Meseguer, J. 2018b Advanced integrated real-time control of  
421 combined urban drainage systems using MPC: Badalona case study. *In: 13th International Conference on*  
422 *Hydroinformatics (HIC), Palermo/Italy, 1-6 July 2018.*
- 423 Sun, C.C., Romero, L.B., Joseph-Duran, B., Meseguer, J., Craviotto, E.M., Guasch, R.P., Martinez, M.P., Puig, V.  
424 & Cembrano, G. 2020 Integrated Pollution-based Real-time Control of Sanitation Systems. *Journal of*  
425 *Environmental Management.* To appear.
- 426 Torres-Matallana, J.A., Leopold, U., Klepiszewski, K. & Heuvelink, G.B.M. 2018 EmiStatR: A Simplified and  
427 Scalable Urban Water Quality Model for Simulation of Combined Sewer Overflows. *Water*, 10, 782.  
428 [doi.org/10.3390/w10060782](https://doi.org/10.3390/w10060782)
- 429 van Rijn, L. 1984 Sediment transport, part II: suspended load transport. *J. Hydra. Engine.*, 110(11), 1613-1641.  
430 [doi.org/10.1061/\(ASCE\)0733-9429\(1984\)110:11\(1613\)](https://doi.org/10.1061/(ASCE)0733-9429(1984)110:11(1613))
- 431 Vezzaro, L., Christensen, M.L., Thirsing, C., Grum, M. & Mikkelsen, P.S. 2014 Water quality-based real time  
432 control of integrated urban drainage systems: A preliminary study from Copenhagen, Denmark. *Procedia*  
433 *Engineering* 70, 1707-1716. [doi.org/10.1016/j.proeng.2014.02.188](https://doi.org/10.1016/j.proeng.2014.02.188)
- 434 Vezzaro, L., Pedersen, J.W., Larsen, L.H., Thirsing, C., Duus, L.B. & Mikkelsen, P.S. 2020 Evaluating the  
435 performance of a simple phenomenological model for online forecasting of ammonium concentrations at WWTP  
436 inlets. *Water Science & Technology*, 81(1), 109-120. [doi.org/10.2166/wst.2020.085](https://doi.org/10.2166/wst.2020.085)
- 437 Wiuff, R. 1985 Transport of suspended material in open and submerged streams. *J. Environ. Eng.* 111(5), 774-792.  
438 [doi.org/10.1061/\(ASCE\)0733-9429\(1985\)111:5\(774\)](https://doi.org/10.1061/(ASCE)0733-9429(1985)111:5(774))