A New Permanent-magnet Vernier In-wheel Motor for Electric Vehicles

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Abstract—This paper proposes a new permanent-magnet vernier (PMV) in-wheel motor to meet the new demands arising from electric vehicles (EVs). It can offer the advantages of light weight, compact size and low-speed high-torque operation. The key is to newly introduce the flux-modulation poles (FMPs) which can effectively modulate the high-speed rotating field of the armature windings and the low-speed rotating field of the PM outer-rotor. By using the time-stepping finite element method (TS-FEM), the performance of the proposed machine can be accurately analyzed. In addition, a prototype is constructed to experimentally verify the simulation results.

I. INTRODUCTION

With ever increasing concerns on fossil energy shortage and global warming, there is fast growing interest in electric vehicles (EVs) [1-3]. Up to now, EVs can be classified as three main types: battery EVs [4, 5], fuel cell EVs [6-8] and hybrid EVs [8, 10]. No matter in which type of EVs, electrical motor is fully or partially substituted for internal combustion engine to drive the vehicles. Thus high performance driving motor has become a core technology for EVs.

In early days, induction motors were preferred for EVs due to their high reliability, manufacturing facilitation and low cost [11-13]. Recently, switched reluctance motors have also been recognized to have considerable potential for EVs because of their simple construction and outstanding torque-speed characteristics [14, 15]. With the advent of high-energy permanent magnets (PMs), some kinds of PM motors have been developed to offer higher power density and operating efficiency, such as PM brushless dc motor [16-21], PM axial flux motor [22-24], PM double salient motor [25-29], PM transverse-flux motor [30, 31] and so on. Some hybrid excitation motor drives have also been proposed to enable the maximum power tracking under different operation state [32-39].

It is well known that for certain power rating, higher rated speed implies smaller motor size as well as lighter weight. Thus in most EV systems, the driving motors are designed to be rated at very high speed (4000rpm or above). However, such motors are demanded to offer high-torque low-speed (around 1000 rpm) operation as well as lightweight and compact design generally. Therefore the motor of the in-wheel EVs system still suffers from the well-known matching problem: the modern high-speed (around 4000rpm) motor, which cannot match with the wheel speed (around 1000 rpm) of EVs. Currently, this problem is handled by either adopting a speed-boost planetary gear [40] or using low-speed machine design [41-43]. The former one causes mechanical wear and tear, audible noise and low efficiency, whereas the latter one increases the generator size and weight as well as raw material cost.

Recently, this matching problem has been solved by integrating a coaxial magnetic gear into a permanent-magnet (PM) motor [41, 44], which allows for directly mounting onto the wheel of EVs to operate at lower speeds. However, this kind of magnetic-gear in-wheel motor desires a complex structure, involving two rotating bodies and three airgaps, which increases manufacture difficulty, cost, the associate transmission loss noise, vibration, and regular lubrication. Its simplified version, namely the magnetic-gearied machine in [45] also has two airgaps.

It is well known that the vernier effect makes it possible to offer low-speed high-torque operation, while avoiding the increase of the number of armature winding pole-pairs [46, 47]. The venier reluctance machine generally has two types, stator-excitation [48, 49], and rotor-excitation [50]. In order to improve the power density, the vernier reluctance machine incorporates PMs to provide the excitation, thus becoming the PM vernier (PMV) machine [51-56].

This paper presents the design of a new kind of PMV motor for the direct-drive of in-wheel EVs. A PMV in-wheel motor was designed in the form of a permanent-magnet vernier outer-rotor motor. The proposed PMV in-wheel motor was simulated by using time steeping finite element method (TS-FEM) to get the steady state parameters. In Section II, the configuration of the proposed PMV in-wheel motor propulsion system will be introduced and the working principle is illustrated. Section III will be devoted to the mathematical model of the proposed PMV in-wheel machine. In Section IV, the finite element analysis of the proposed machine will be presented and the machine performances will be assessed. Hence, its validity will be verified quantitatively. Finally, conclusion will be drawn in Section V.

II. PRINCIPLE OF OPERATION

Fig.1 shows the schemes of the outer-rotor PMV in-wheel motor when it serves as the in-wheel motor drive for EVs, especially for motorcycles. It can be seen that these in-wheel motor drives effectively utilize the outer-rotor nature and is directly coupled with the tire rims. So, this topology can fully utilize the space, hence greatly reducing the size and weight of the drive system for EV applications.
By borrowing the concept of magnetic gears and the outer-rotor arrangement of other machines, the proposed PMV in-wheel machine is shown in Fig. 2 and the corresponding prototype is shown in Fig. 3. The key is to newly introduce the flux-modulation poles (FMPs) into the outer part of the inner stator, which resemble the ferromagnetic segments of the stationary ring in the coaxial magnetic gear, to modulate the high-speed rotating field of the armature windings and the low-speed rotating field of the PM outer-rotor. Similar to the magnetic gear or other PMV machines, the number of pole-pairs in the space harmonic flux density distribution produced by either the high speed rotating field of the armature winding and the low rotating field of the rotor permanent magnets, is given by:

$$ p_r = N_s - p_s $$

(1)

where $N_s$ is the number of FMPs, $p_r$ is the number of rotor PM pole-pairs and $p_s$ is the number of armature winding pole-pairs. Consequently, the high-to-low speed ratio $G_r$ is given by:

$$ G_r = \frac{m p_r + k N_s}{m p_s} $$

(2)

where $m = 1,3,\ldots$ and $k = 0,\pm 1,\pm 2,\ldots$.

Compared with the previous designs, the proposed machine takes the following advantages:

- This structure involves only one airgap, which is much simpler than the magnetic-gearred machine structure (involving three airgaps) [40, 44], and the other PMV machine (involving two airgaps) [46].
- The outer-rotor arrangement inherently provides a large diameter to accommodate a large number of PM poles, and enables full utilization of the inner space for the stator to accommodate the armature windings, thus eliminating the problem of large vacancy in the double excitation PMV machine [46].
- The outer rotor allows for direct coupling with the wheel, which can alleviate the bearing requirements and improving the mechanical integrity.
- The inner-stator arrangement with FMPs enables to adopt compact armature windings, therefore avoiding the problem of drum windings used in [46]. Also, the armature windings adopt the coil pitch equal to the slot pitch, which can minimize the end-windings, hence saving the copper material and reducing the copper loss.

## III. ANALYSIS APPROACH

The TS-FEM is employed to analyze the system performances. It has been verified that it is an efficient way to analyze the motor drives [57]. Firstly, the electromagnetic field equation of the machine is governed by:

$$ \Omega : \frac{\partial}{\partial x} \left( v \frac{\partial A}{\partial x} \right) + \frac{\partial}{\partial y} \left( v \frac{\partial A}{\partial y} \right) = -i + \left( \frac{\partial B_{rx}}{\partial x} + \frac{\partial B_{ry}}{\partial y} \right) + \sigma \frac{\partial A}{\partial t} $$

(3)

where $\Omega$ is the boundary of calculation, $A$ is the magnetic vector potential component along the z-axis, $J$ is the current density, $v$ is the reluctivity, $\sigma$ is the electrical conductivity, $B_{rx}$ and $B_{ry}$ are the remnant flux density components of the PM rotor. From (2), it yields $G_r = -8:1$, namely the rotor speed is only 1/8 of that in the conventional machine with the same number of armature winding pole-pairs and stator slots, but rotating in an opposite direction. Therefore, when the speed of rotating field in the stator is 8000 rpm, the outer rotor speed is scaled down to 1000 rpm.
along the \( x \) and \( y \) axes respectively.

**A. In the Airgap and the Iron Cores**

The field equation expressed in the 2-D Cartesian
coordinates, in regions without source current and PM is
\[
\Omega_1: \frac{\partial}{\partial x} \left( v \frac{\partial A}{\partial x} \right) + \frac{\partial}{\partial y} \left( v \frac{\partial A}{\partial y} \right) = 0
\]
(4)

where \( \Omega_1 \) is the region of the airgap and the iron cores, \( A \) is the axial component of the magnetic vector potential, and \( v \) is the reluctivity of the material.

**B. In the Stranded Windings**

In the armature winding where the current density is
uniform, the field equation is
\[
\Omega_2: \frac{\partial}{\partial x} \left( v \frac{\partial A}{\partial x} \right) + \frac{\partial}{\partial y} \left( v \frac{\partial A}{\partial y} \right) = -\frac{i}{S}
\]
(5)

where \( K_r \) is the polarity (+1 or −1) to represent either the forward paths or return paths, \( i \) is the stator phase current, \( S \) is the conductor area of each turn of armature winding, and \( \Omega_2 \) represent the region of forward paths and return paths of the conductor.

**C. In the PMs**

In the PM region, the total current \( i_o \) in each piece of the PM should be zero. The field equation is given by
\[
\Omega_3: \frac{\partial}{\partial x} \left( v \frac{\partial A}{\partial x} \right) + \frac{\partial}{\partial y} \left( v \frac{\partial A}{\partial y} \right) = \nu \left( \frac{\partial B_{r0}}{\partial x} + \frac{\partial B_{r0}}{\partial y} \right)
\]
(6)

where \( \Omega_3 \) is the boundary of the PMs, \( \nu \) is the reluctivity of the material, \( B_{r0} \) and \( B_{r0} \) are the \( x \)-axis and \( y \)-axis components of the PM remnant flux density respectively.

Secondly, the armature circuit equation of the machine is expressed as [58]:
\[
u = Ri + L \frac{di}{dt} + e
\]
(7)

where \( i \) is the stator phase current, \( R \) is the stator winding resistance, \( L \) is the inductance of the armature windings, \( S \) is the sectional area of the conductor of each phase, and \( e \) is the branch voltage of the winding. The induce electromotive force (EMF) in the winding is
\[
e = -\frac{l}{S} \int_{x'} \frac{\partial A}{\partial t} d\Omega + \frac{l}{S} \int_{x'} \frac{\partial A}{\partial t} d\Omega
\]
(8)

If (5) and (7) are directly coupled together, the coefficient matrix of the system equations will become asymmetrical in the nodal analysis [58, 59]. Consequently, an additional unknown in the stranded windings is proposed below in order to make the coefficient matrix symmetrical.

Using the backward Euler’s method [60] to discretize the time variable, one gets
\[
\frac{di^k}{dt} = i^k - i^{k-1}
\]
(9)

where, the superscript \( k \) is the step number in the time stepping process, \( i^k \) is the stator phase current in the \( k \) th step, and the step size \( \Delta t = t^k - t^{k-1} \). Substituting the above equation into (7), one has

\[
i^k = \left( -e - L \frac{\Delta i^k}{\Delta t} \right) \left( R + \frac{L}{\Delta t} \right)
\]
(10)

Substituting (10) into (7), the field equation is
\[
\frac{l}{S} \left( R + \frac{L}{\Delta t} \right) i^k = \frac{l}{S} \left( R + \frac{L}{\Delta t} \right) i^{k-1} - \frac{L}{S} \Delta t \left( R + \frac{L}{\Delta t} \right) i^{k-1}
\]
(11)

Then substituting (8) and (10) into (7), the branch equation is

\[
i^k = \frac{l}{S} \left( R + \frac{L}{\Delta t} \right) \int_{x'} \frac{\partial A}{\partial t} d\Omega + \frac{1}{S} \left( R + \frac{L}{\Delta t} \right) e = 0
\]
(12)

Equation (8) can also be written as,
\[
i^k = \frac{l}{S} \left( R + \frac{L}{\Delta t} \right) \int_{x'} \frac{\partial A}{\partial t} d\Omega + \frac{1}{S} \left( R + \frac{L}{\Delta t} \right) e = 0
\]
(13)

Thirdly, the motion equation is given by:
\[
\frac{l}{\mu_o} \int r^2 B_r d\theta = T + J \frac{d\omega}{dt} + B \omega
\]
(14)

where \( J \) is the moment of inertia, \( \omega \) is the rotor speed, \( T \) is the mechanical driving torque, \( T_e \) is the electromagnetic torque, and \( B \) is the damping coefficient.

By coupling the field equation (3), voltage equation (7) and the motion equation (14), the TS-FEM can be performed to calculate both the steady-state and dynamic performances of the motor.

**IV. PERFORMANCES OF THE PROPOSED MACHINE**

In order to illustrate the validity of the proposed machine, its performances are quantitatively analyzed by TS-FEM. The overall outside diameters, axial lengths, total copper volume and PM volume are listed in Table 1. It can be found that the proposed machine possesses the large rated power and low rated speed for directly driving in-wheel EVs. This merit is actually due to the proposed PMV structure which can significantly improve the power density.

**TABLE I**

<table>
<thead>
<tr>
<th>DESIGN DATA OF THE PMV IN-WHEEL MACHINE</th>
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<tbody>
<tr>
<td>Items</td>
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<tr>
<td>-------------------------------</td>
</tr>
<tr>
<td>Rated power</td>
</tr>
<tr>
<td>Rated phase voltage</td>
</tr>
<tr>
<td>Rated current</td>
</tr>
<tr>
<td>Rated speed</td>
</tr>
<tr>
<td>Gear ratio</td>
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<tr>
<td>No. of armature winding poles</td>
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<tr>
<td>No. of stator poles</td>
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<tr>
<td>No. of FMPs</td>
</tr>
<tr>
<td>No. of rotor poles</td>
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<tr>
<td>Overall outside diameter</td>
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<tr>
<td>Shaft diameter</td>
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<tr>
<td>Axial length</td>
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</tbody>
</table>
Fig. 4 shows the magnetic field distributions of the proposed machine under no-load. It can be observed that the flux lines per stator tooth of the proposed machine can pass through the FMPs separately, hence verifying the desired flux modulation. Furthermore, the flux lines concentrated in six poles so that the output torque is more effective.

The airgap flux density waveforms are shown in Fig. 5. From the figure, the averaged peak value of the proposed machine is 0.856 T and the maximum value is 1.015 T, quantitatively. It also can be seen that the proposed machine has 24 pole-pairs in the airgap within 360° which corresponds to 24 pole-pairs of the PMs on the rotor, thus well agreeing with each other. In addition, there are several peaks that have higher amplitudes than others as marked in the figure. This is because at some points, the N poles or S poles happen to face or nearly face the FMPs on the stator, while at some other points, the PM poles happen to object to the stator slots.
Due to the use of PMs, the PMV in-wheel motor can definitely produce high torque while operating at low rotational speed. This characteristic can benefit to the application of direct-drive in-wheel EVs.

Fig. 9 shows the back EMF waveforms of the proposed PMV in-wheel motor at the rated speed of 1000 rpm. It can be found that the root mean square (RMS) value of the proposed machine is 427.66 V. Fig. 10 shows the corresponding harmonic spectra of the back EMF, and it can be seen from Fig. 10 that the amplitude of the harmonics is very small. The base frequency is 400 Hz and the harmonics are mainly generated by the FMPs. Fig. 11 shows steady state torque at rated speed. The average output torque is 16.011 N. Due to the use of PMs, the PMV in-wheel motor can definitely produce high torque while operating at low rotational speed. This characteristic can benefit to the application of direct-drive in-wheel EVs.

**V. CONCLUSION**

In this paper, a novel PMV in-wheel machine has been developed for direct-drive EVs, which can offer low-speed operation to directly coupled to the wheel, and enable high-speed rotating field design to maximize the power density. Compared with its mechanical gear counterpart, the proposed machine can eliminate the mechanical wear and tear as well as transmission loss, thus improving the generation reliability and efficiency. Compared with its PMV counterparts, it offers higher power density and higher output voltage, while reducing the raw material volume and hence the overall cost. By using the TS-FEM, the proposed machine is quantitatively analyzed in terms of back EMF generation and torque-handling capability, thus verifying that it is very promising for direct-drive application in EVs.

**ACKNOWLEDGMENT**

This work was supported by a grant (Project No. HKU7105/07E) from the Hong Kong Research Grants Council, Hong Kong Special Administrative Region, China.

**REFERENCES**


